



φ -FACTORABLE OPERATORS AND WEYL-HEISENBERG FRAMES ON LCA GROUPS

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ABSTRACT. We introduce φ -frames in $L^2(G)$, as a generalization of a -frames defined in [7], where G is a locally compact abelian group and φ is a topological automorphism on G . We give a characterization of φ -frames with regard to usual frames in $L^2(G)$ and show that φ -frames share several useful properties with frames. We define the associated φ -analysis and φ -preframe operators, with which we obtain criteria for a sequence to be a φ -frame or a φ -Bessel sequence. We also define φ -Riesz bases in $L^2(G)$ and establish equivalent conditions for a sequence in $L^2(G)$ to be a φ -Riesz basis.

1. INTRODUCTION AND PRELIMINARIES

The theory of frames was introduced by Duffin and Schaeffer [10] in the early 1950s to deal with problems in nonharmonic Fourier series. There has been renewed interest in the subject related to its role in wavelet theory and a lot of new applications. Several kinds of frames have been introduced up to now; e.g. frames in Hilbert C^* -modules (modular frames) [14], frames of subspaces [8], G -frames [26], p -frames [1], frames for Banach spaces [6], a -frames [7], and many others for different purposes. In this paper we define and investigate φ -frames in $L^2(G)$, using the φ -bracket product, as a vector valued inner product on $L^2(G)$ introduced in [19], where G is a locally compact abelian (which will be abbreviated to "LCA ") group and φ is a topological automorphism on G . One of

2000 *Mathematics Subject Classification*. Primary 43A15; Secondary 43A25, 42C15.

Key words and phrases. φ -bracket product, φ -factorable operator, φ -frame, φ -Riesz basis, locally compact abelian group .